Atom Interferometry with the Sr Optical Clock Transition

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We report on the realization of a matter-wave interferometer based on single-photon interaction on the ultranarrow optical clock transition of strontium atoms. We experimentally demonstrate its operation as a gravimeter and as a gravity gradiometer. No reduction of interferometric contrast was observed for a total interferometer time up to \(\sim 10\) ms, limited by geometric constraints of the apparatus. Single-photon interferometers represent a new class of high-precision sensors that could be used for the detection of gravitational waves in so far unexplored frequency ranges and to enlighten the boundary between quantum mechanics and general relativity.

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Matter-wave interference enables the investigation of physical interactions at their fundamental quantum level and forms the basis of high-precision inertial sensors and for application in precision gravitational field sensing [1]. Today’s best atom interferometers (AIs), based on multi-photon Raman or Bragg transitions and Bloch oscillations, can tailor matter waves at will, up to macroscopic scales [2], preserving their coherence for extremely long times [3], allowing precision measurements of the Newtonian gravitational constant [4], Earth gravity acceleration [5,6], gravity gradients [8,9], and gravity curvature [10,11]. At the same time, optical spectroscopy of ultranarrow optical transitions in atoms and ions has produced clocks with the highest relative frequency accuracy, approaching the \(10^{-19}\) level [12–15]. Thanks to these impressive results, schemes for gravitational waves detectors based on AIs and optical clocks have been proposed [16–23].

In this Letter, we demonstrate atom interferometry based on the ultranarrow \(^1S_0\to^3P_0\) optical clock transition of \(^{88}\)Sr at \(\lambda = 698\) nm both for a single AI (gravimeter) and for two simultaneous AIs in a differential scheme (gravity gradiometer). While atom interferometry based on intercombination transitions of calcium and magnesium has been reported already [24–27], the virtually infinite lifetime of the upper clock state in strontium is crucial for demanding applications. For example, as proposed in Refs. [18,19], the differential scheme demonstrated here might allow us to detect gravitational waves in the low-frequency range using a single-arm large-scale AI. This novel sensor will also enable new fundamental tests lying at the border of quantum mechanics and general relativity [28,29], such as the quantum interference of clocks, with the possible observation of the redshift induced decoherence effects [30,31], a light dark matter search [32], and tests of the weak equivalence principle with quantum superpositions of states with large energy (\(\sim\)eV) separation [33]. Precision measurements of gravity will also be necessary for the development of optical lattice clocks. The comparisons of clocks at the \(10^{-19}\) level will not only require a precise knowledge of the static gravitational field component at the atomic cloud location, but it will also demand a simultaneous measurement of time-varying gravitational potential effects down to the exceptional level of \(10^{-2} m^2/s^2\) [34]. Novel single-photon AIs, based on the same atomic transition employed as a frequency reference in optical lattice clocks, will then play an important role in this field by enabling advanced experimental sequences with interleaved precision measurements of the optical frequency and the gravitational potential.

In our experiment, a Mach-Zehnder-type AI is generated by the interaction of the freely falling Sr atoms with a \(\pi/2,\pi,\pi/2\) sequence of laser pulses whose frequency \(\omega\) is resonant with the optical atomic clock frequency \(\omega_a\) (Fig. 1). The phase shift \(\Delta \Phi\) between the two AI arms is given by [19,35]

\[
\Delta \Phi = \left(\alpha - \frac{\omega}{c}\right)T^2 \left[1 + \left(2 + \frac{4}{\pi}\right)\frac{\tau}{T} + \frac{8}{\pi}\left(\frac{\tau}{T}\right)^2\right] + (\phi_1 - 2\phi_2 + \phi_3),
\]

where \(\tau\) is the duration of the \(\pi/2\) pulse, \(T\) is the free-fall time between two subsequent pulses, \(\alpha\) is the frequency chirping rate applied to the clock laser pulses to compensate for the gravity-induced Doppler shift, and \(\phi_i = \omega z_i/c - \omega t_i\) are the phases of the clock laser field at positions \(z_i\) and times \(t_i\) at the beginning of each optical pulse.

The implementation of a single-photon AI poses several challenges. High-power and high-frequency-stability laser systems are required to drive the high-\(Q\) optical clock transition with a sufficiently high Rabi frequency. This condition is even more stringent in the case of large momentum transfer beam splitters [19,36]. As Eq. (1) shows, single-photon AIs are sensitive to the optical phase
of the clock laser field, that is, to the phase difference of the laser field with respect to the atomic phase, rather than to the phase difference between two laser fields, as in multi-photon Raman or Bragg AIs. This sets stringent requirements on the phase stability of the laser employed to drive the clock transition. For instance, a small fluctuation in the optical path ~200 nm between the clock laser and the atoms induces a phase change larger than π/2 that is large enough to mask the AI signal. Therefore, to exploit the benefit of using the clock transition in atom interferometry, techniques to actively cancel the phase noise of the optical field or differential interferometric schemes need to be employed.

To drive the optical clock transition, we employed a 1 Hz–linewidth laser delivering up to 350 mW at λ = 698 nm. The system is based on a master laser frequency stabilized to a high finesse cavity [37]; it is power amplified by a slave laser and a tapered amplifier. For the double-cloud (gradiometer) experiments, the clock laser includes two frequency components ω1 and ω2 in order to simultaneously interact with both atomic samples. This is implemented by passing the clock laser beam in an acousto-optical modulator fed with two frequencies produced by a two-channel direct digital synthesizer generator. The AI pulses at different frequencies share the same optical path including fiber, mirrors, and optics, then acquiring only common-mode noise. With a 1/e^2 beam radius of 500 μm, the typical peak intensity of each frequency on the atoms is about 10 W/cm^2.

The experiment was performed using the most abundant isotope of strontium, ⁸⁸Sr, for which the J = 0 – J = 0 optical clock transition is strictly forbidden but can be induced and tuned in its strength by a static magnetic field

The procedure to produce ultracold samples of strontium has been described elsewhere [3,39]. In brief, a cloud of ~5 × 10⁶ ultracold ⁸⁸Sr atoms at a temperature of 1.2 μK, with a horizontal (vertical) dimension of 300 μm (70 μm) at full width at half maximum, is produced by a two-stage magneto-optical trap (MOT). After the MOT cloud preparation stage, about 50% of the atoms are loaded into a vertical 1D optical lattice at 532 nm. The atoms are maintained in the trap for a time of about 65 ms, which is necessary to invert the current direction in one of the MOT coils in order to produce a homogeneous magnetic field

The procedure to launch the atoms into the fountain is different for the case of a single cloud and for the double cloud: In the first case, the atoms are released from the trap by switching off adiabatically the lattice beam and fall freely. For the two-cloud configuration, we extended the technique used in Ref. [39] to perform a double launch from a single source: about 10% of the atoms in the lattice are accelerated vertically upwards in 8 ms by ramping down the frequency of the top lattice beam at a rate of 100 kHz/ms, corresponding to an acceleration of 2.7g; the remaining atoms are retrapped after a variable free-fall time and a second cloud is launched upwards with the same method in 6 ms. With a free-fall time of 1 ms, we produce two clouds with a similar number of atoms (~2.5 × 10⁵), a separation Δr₀ = 1.9 mm (limited by geometric constraints of the apparatus), and a velocity difference Δv₀ = 5.3ℏω₀/mc along the vertical axis (where m is the mass of the ⁸⁸Sr atom) leading to a slight increase of 0.3 mm in the cloud distance during the subsequent AI stage.

The atoms launched in the fountain are velocity selected in the vertical direction with a π pulse resonant with the clock transition. The remaining atoms in the ground state are blown away using light resonant with the dipole-allowed ¹S₀–¹P₁ transition at 461 nm. Typically, about 4% of the atoms are selected, thus producing samples of about 10⁸ atoms with a narrow vertical momentum width of ~0.04ℏω₀c (Fig. 2). This shows that an ultranarrow clock transition can provide a free-falling ensemble of atoms with a very well-defined velocity, enabling high AI contrast [40].

After the velocity selection, the AI π/2–π–π/2 laser pulse sequence resonant with the optical clock transition is applied to the atoms. In this way, atomic “internal”
observed fringe contrast and visibility with and without actively stabilizing the clock laser phase at the fiber end [41,42]. The main sources of phase noise are indeed acoustic and subacoustic vibrations coupled to the atomic system and to the 10 m–long polarization maintaining fiber used to bring the clock laser light to the atoms. The active fiber noise cancellation (FNC) system has a bandwidth of 50 kHz, reducing by more than 50 dB the phase noise up to 100 Hz [inset in Fig. 3(e)]. With this system, we observed a dramatic difference for the fringe visibility when the FNC is active (Fig. 3). This is particularly clear for the fringes corresponding to the longest AI time. The fringe visibility is only partially recovered by the FNC system, as shown in Fig. 3(d), because of uncompensated phase noise introduced by the optical components outside the loop before the atomic cloud.

The observed AI visibility and contrast are affected by the \( \pi \)-pulse efficiency \( \sim 50\% \) [Fig. 2(b)] limited mainly by the initial atomic momentum width. The pulse duration for the momentum selection is indeed a trade-off between the number of selected atoms and the momentum width. A longer selection pulse would lead to an increase of the \( \pi \) pulse efficiency at the expense of the final atom number in the AI. The chosen parameters are the results of an optimization of the signal-to-noise ratio at the final detection. Further reduction of the contrast is due to clock laser intensity inhomogeneity (the clock beam size is comparable to the atomic cloud size) and to the residual motion of the atoms during the \( \sim \)millisecond long \( \pi \)-pulse time. Using the fermionic \( ^{87}\)Sr isotope with the same laser intensity, the Rabi frequency would be \( \Omega \sim 2\pi \times 5 \) kHz, thus allowing a larger laser beam size or a shorter \( \pi \)-pulse duration. With a single-frequency clock laser peak intensity on the atomic

(electronic) clock states and “external” (momentum) states are entangled. At the end of the AI sequence, a push beam resonant with the intercombination (electronic) clock states and

\[
\sinusoid \text{ with a corresponding Rabi frequency of } \Omega = \frac{\pi}{\Delta}, 
\]

are resorted with the intercombination (electronic) clock states and

\[
\text{an atomic momentum spread of } \sqrt{\frac{\hbar}{2m\delta\omega}}. 
\]

The oscillation is recorded with typical values of the static magnetic field \( (B = 330 \text{ G}) \) and clock light peak intensity \( (20 \text{ W/cm}^2) \). The experimental result fits well with a damped sinusoid with a corresponding Rabi frequency of \( \Omega = 2\pi \times 753(30) \text{ Hz} \) and a damping time of \( 1.18(0.15) \text{ ms} \).

The interference fringes obtained for the single AI (gravimeter) are shown in Fig. 3. We compared the

FIG. 2. (a) Clock spectroscopy signal on the free-falling, momentum selected cloud. The signal linewidth, by eliminating the effect of the finite spectroscopy pulse length \((1.2 \text{ ms})\) and estimated from a Gaussian fit of the profile, indicates an atomic momentum spread of \( 0.04\hbar\omega_a/c \). (b) Rabi oscillations of the atomic excitation fraction as a function of the clock pulse length. The oscillation is recorded with typical values of the

FIG. 3. Results for the single AI (gravimeter). AI fringes in (a) and (b) were observed for \( 2T = 2 \text{ ms} \), with and without the active fiber noise cancellation (FNC) system, respectively; AI fringes in (c) and (d) correspond to \( 2T = 10 \text{ ms} \), with and without FNC, respectively. (e) Measured contrast and fringe visibility as a function of \( 2T \). Fringe visibility (red open squares and circles) is given by the amplitude of the fitted sinusoidal function on each data set. Contrast (solid squares and circles) is estimated by data dispersion from the 2nd to the 98th percentile. Both contrast and visibility are measured with (squares) and without (circles) FNC. The inset shows the in-loop phase noise power spectral density of the 10 m–long optical fiber connecting the clock laser source to the AI, with (lower red curve) and without (upper black curve) FNC, respectively.
sample of about 20 W/cm² and a maximum static magnetic field $B = 330$ G, the observed Rabi frequency is $\Omega = 2\pi \times 753(30)$ Hz, corresponding to a $\pi$-pulse duration $\tau_p = 0.7$ ms [see Fig. 2(b)]. While this value is larger than the typical Raman or Bragg pulse duration, it is important to notice that in the case of single-photon clock interaction, the losses due to spontaneous emission are largely reduced. This represents a considerable advantage with respect to two-photon Raman or Bragg pulses, where the spontaneous emission constitutes a major limitation to AI contrast so that short pulses and large detunings from the single-photon transition are typically required.

Results obtained for the two simultaneous AIs (gravity gradiometer) are shown in Fig. 4. In order to study the common-mode phase noise rejection in the differential configuration, data have been acquired without FNC. For the gravity gradiometer, the differential phase shift is given by [43,44]

$$
\Delta \phi \approx \frac{\omega}{c} (\Gamma T^2) \Delta r_0 + \frac{\omega}{c} (\Gamma T^2) \Delta v_0 T + \delta \phi \equiv \delta \phi_0 + \delta \phi_v + \delta \phi_r,
$$

where $\Gamma$ is the gravity gradient. The first two leading phase shift terms are induced by the separation $\Delta r_0$ and the velocity difference $\Delta v_0$ between the two clouds, corresponding to $\delta \phi_r \sim 10^{-6}$ rad and $\delta \phi_v \sim 10^{-7}$ rad for $T = 5$ ms, that are too small to be measured with our current sensitivity. This would result in a closed ellipse pattern when plotting the interference fringe signals of one AI versus the other, thus preventing a fitting of the data. In order to analyze the data, a synthetic phase $\delta \phi$ was introduced by adding a relative phase shift between the two radio-frequency signals used to drive the acousto-optical modulator acting on the clock laser beam. In this case, the observed ellipse angle will be the sum of the synthetic phase $\delta \phi$ and the other phase contributions. Compared to other methods, in which a relative phase shift $\delta \phi$ is introduced via artificial external gradients [43,45], here no additional fields or changes of the pulse wave number are required.

The effective suppression of common-mode phase noise in the gradiometer configuration is apparent when comparing the signals in Figs. 3 and 4; we estimate a suppression by at least 20 dB in the relevant frequency range. We characterized the gradiometer short-term sensitivity via the Allan deviation of the relative phase shifts for 1300 cycles for $2T = 2$ ms and $2T = 10$ ms (Fig. 4). The cycle time was set to 2.4 s, resulting in an overall acquisition time of about 1 h, for each set. Each ellipse was fit on 11 successive points. We find that the Allan deviation scales as the square root of the averaging time, showing that the residual noise is from white phase noise. The relative phase sensitivity at 400 s is approximately 82 mrad, which is 5 times higher than the shot-noise-limited sensitivity estimated for $10^4$ atoms and with a typical contrast of $\sim 30\%$. The current sensitivity is indeed limited by the photon collection efficiency at the output of the AI.

In conclusion, we have experimentally demonstrated a novel AI based on the ultranarrow clock transition of $^{88}$Sr atoms. We implemented the scheme for a single AI (gravimeter) and for two simultaneous AIs (gravity gradiometer). We showed that the laser phase noise is drastically reduced in the gradiometric configuration, enabling the retrieval of the fringe visibility and contrast for an AI duration up to $\sim 10$ ms, limited by the present apparatus. The lattice double-launch technique and high frequency selectivity of the optical clock transition that we implemented allowed us to add a synthetic relative phase shift $\delta \phi$ with a novel method.

The new atom interferometry scheme we demonstrated will be important to investigate effects at the boundaries of quantum mechanics and general relativity. In the future, the implementation of this scheme in very-long-baseline gravimeters might allow us to detect gravitational waves in the so far unexplored low-frequency range. The clock transition in $^{87}$Sr is also being considered for precision atom interferometry with atoms in optical waveguides [46].

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